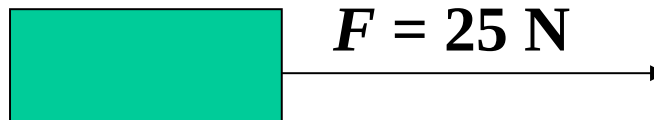


TEKOČINE

togo telo:

m, F



$$m = 3,6 \text{ kg}$$

tekočina:

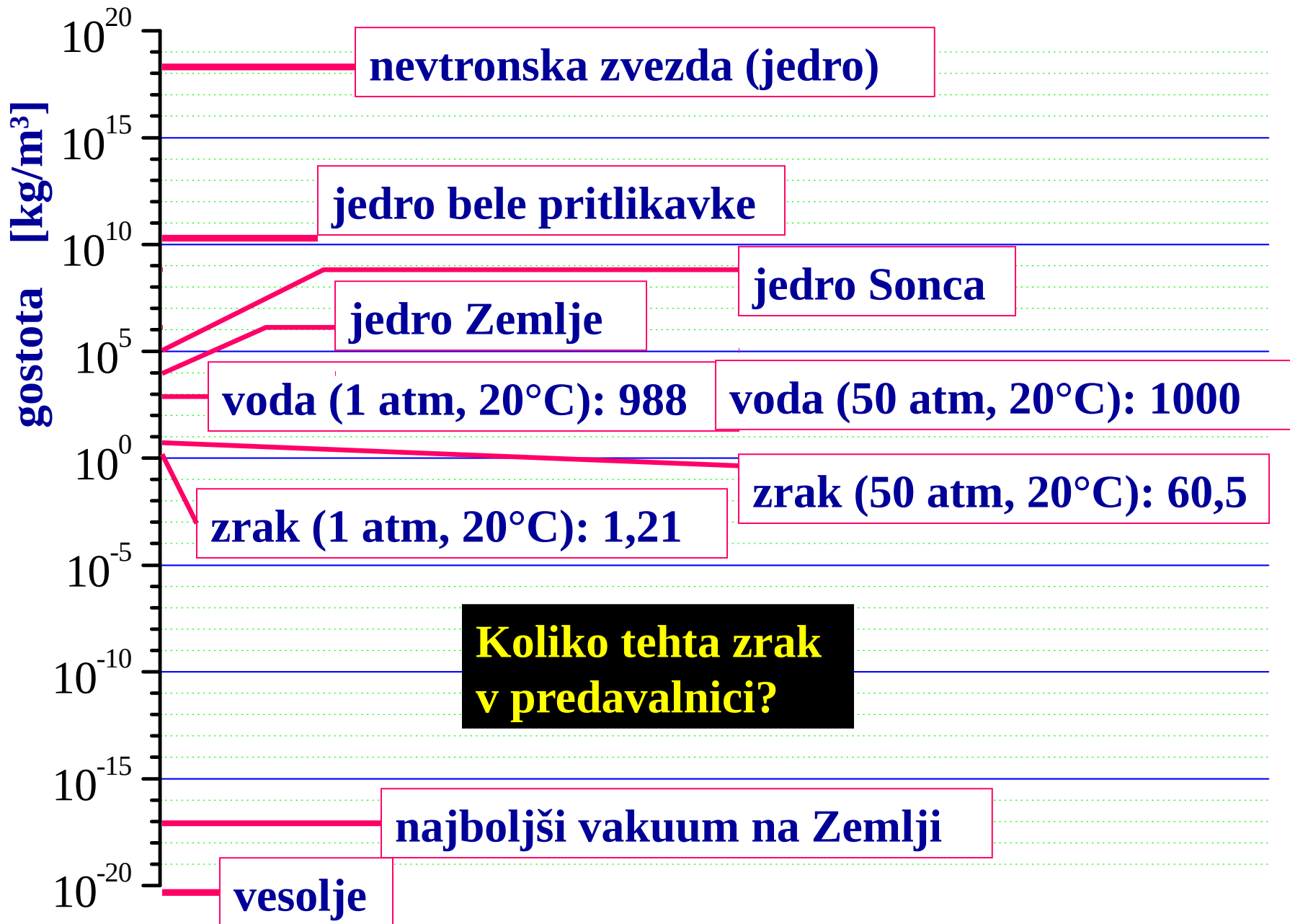
gostota, tlak

GOSTOTA

$$\rho = \frac{\Delta m}{\Delta V} \left[\frac{\text{kg}}{\text{m}^3} \right]$$

homogen vzorec

$$\rho = \frac{m}{V}$$



GOSTOTA

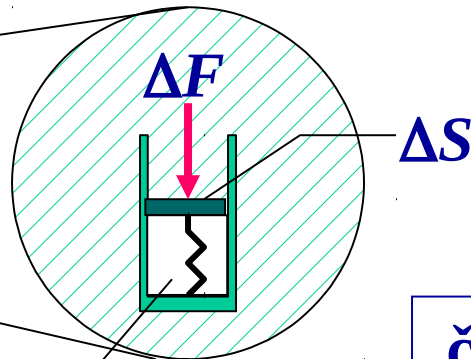
$$\rho = \frac{\Delta m}{\Delta V} \left[\frac{\text{kg}}{\text{m}^3} \right]$$

homogen vzorec

$$\rho = \frac{m}{V}$$

TLAK

**merilnik
tlaka**



vakuum

$$p = \frac{\Delta F}{\Delta S}$$

**če je sila enaka
po vsej površini**

$$p = \frac{F}{S}$$

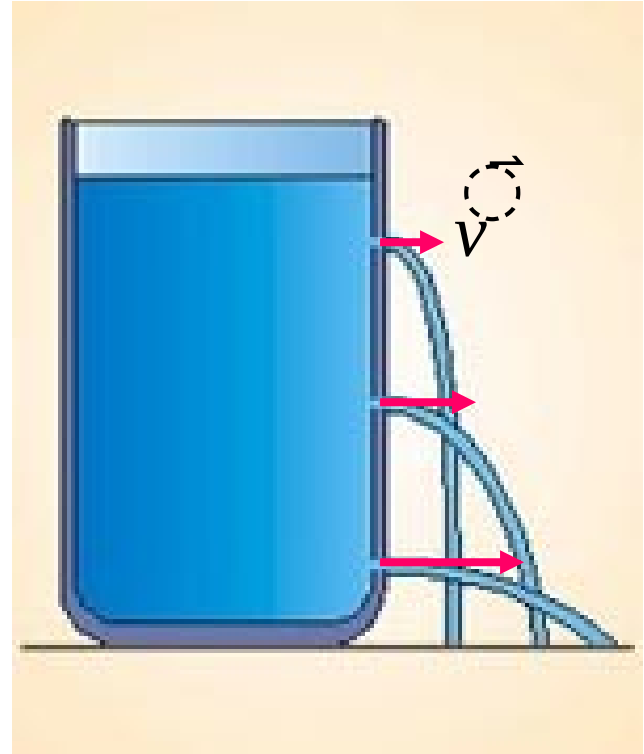
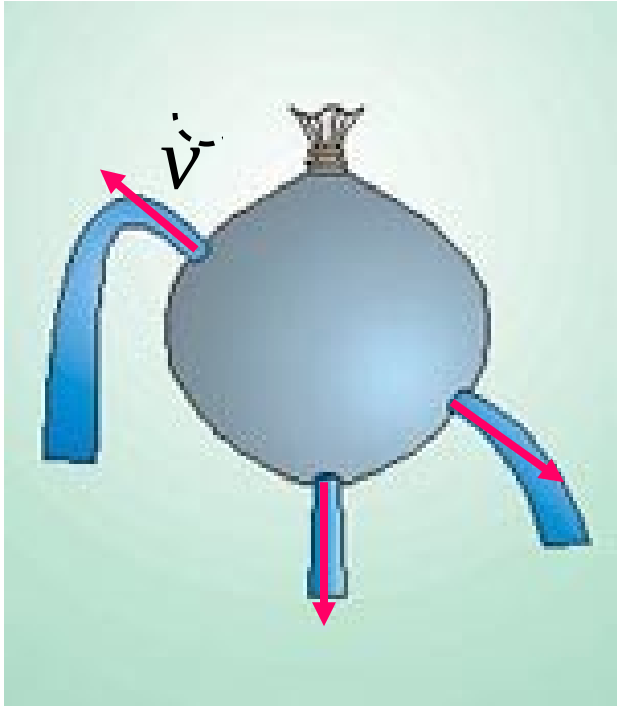
enota:

$$\left[\frac{\text{N}}{\text{m}^2} = \text{Pa} \right]$$

paskal

skalarna količina

$$1 \text{ atm} = 1,01 \cdot 10^5 \text{ Pa} = 760 \text{ torr} = 760 \text{ mmHg}$$



[Pa]

središče Sonca

10^{15}

10^{12}

središče Zemlje

10^9

najvišji tlak dosežen v laboratoriju

10^6

atmosferski tlak

10^3

krvni tlak (tlak nad atm. tlakom)

10^0

S kolikšno silo deluje atmosfera na tla v predavalnici?

10^{-3}

10^{-6}

10^{-9}

10^{-12}

najboljši vakuum ustvarjen na Zemlji

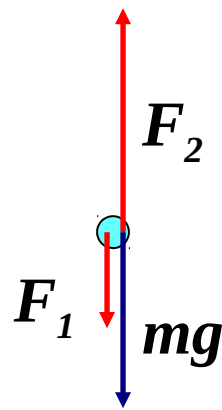
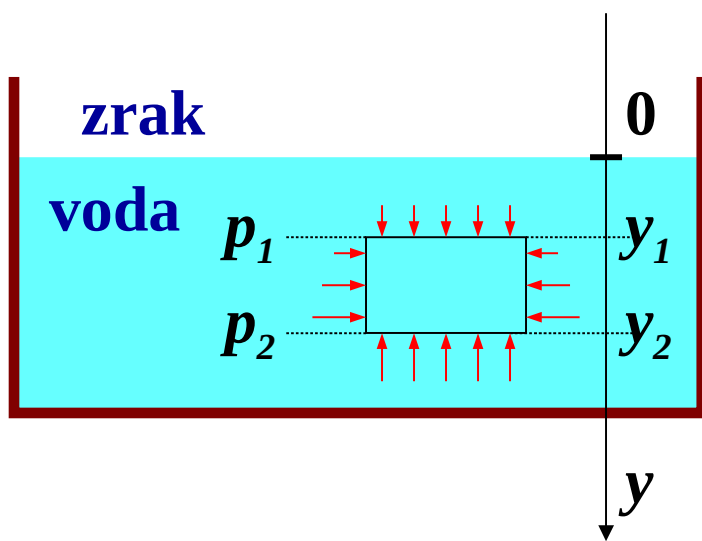
t
l
a
k

TEKOČINE V MIROVANJU - HIDROSTATIKA

potapljač: tlak narašča z globino

alpinist: tlak se manjša z višino

hidrostatični tlak

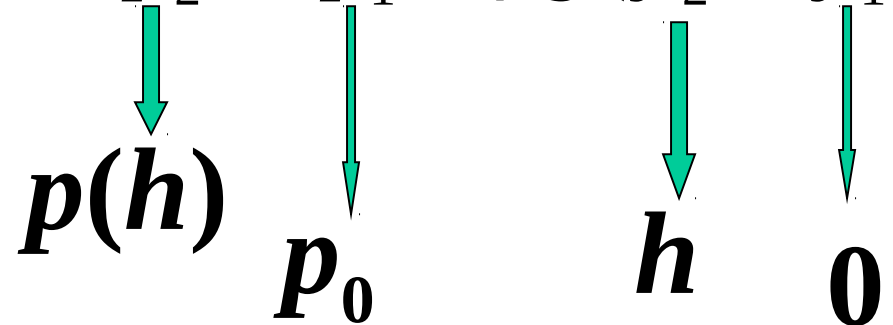


$$F_2 = p_2 S$$

$$F_1 = p_1 S$$

$$F_2 = F_1 + mg$$

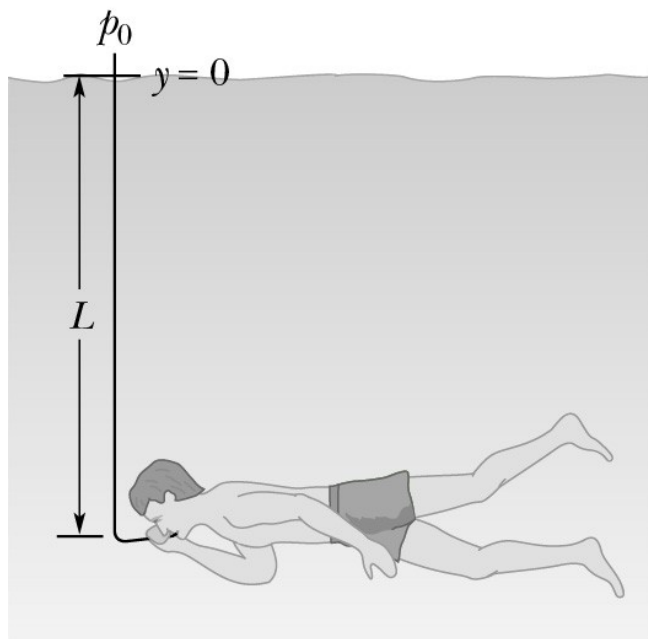
$$p_2 = p_1 + \rho g (y_2 - y_1)$$



$$p(h) = p_0 + \rho g h$$

zračni tlak na površini vode

PRIMER:



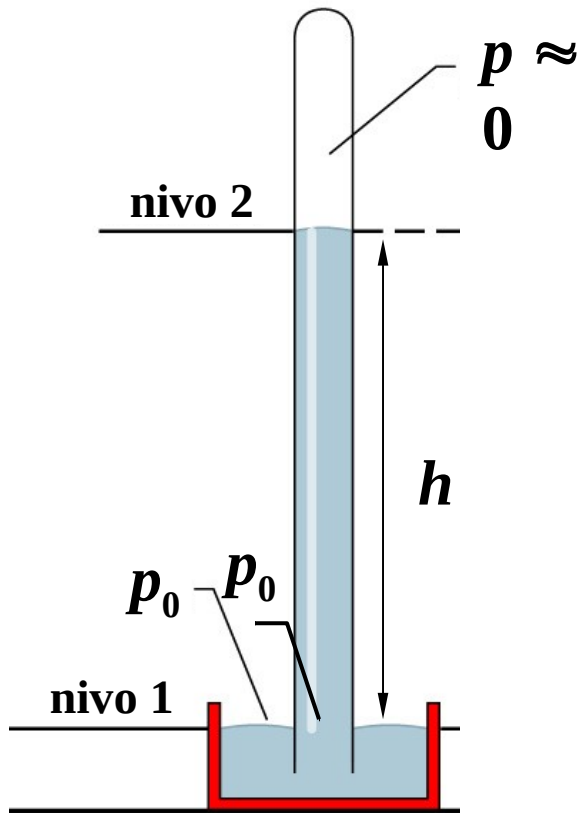
Nespameten potapljač razmišlja: če deluje 20 cm dolga dihalka, deluje tudi **6,0 m dolga cev**. Če tako cev res uporabi, je **v smrtni nevarnosti!!!** Zakaj?

PRIMER:

Potapljač začetnik **zajame zrak na dnu bazena z globino 1,0 m**. Ko se **dviguje, pozabi izdihovati**. Zakaj je **v smrtni nevarnosti**?

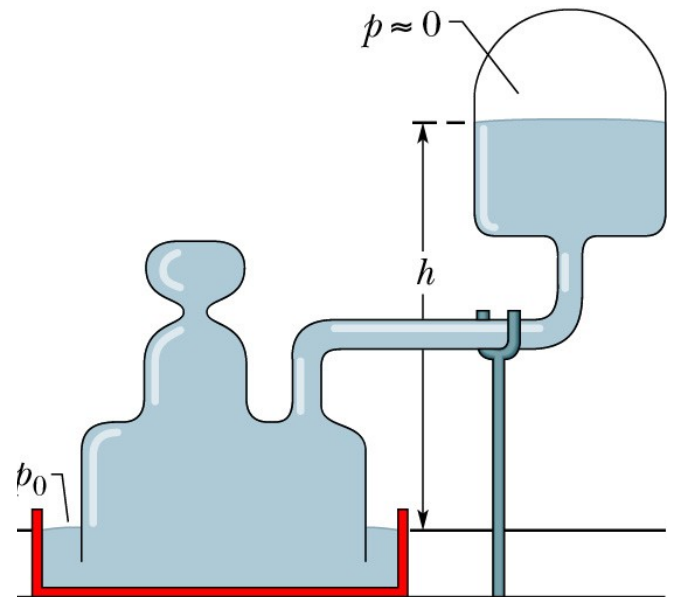
MERJENJE TLAKA

živosrebrni barometer

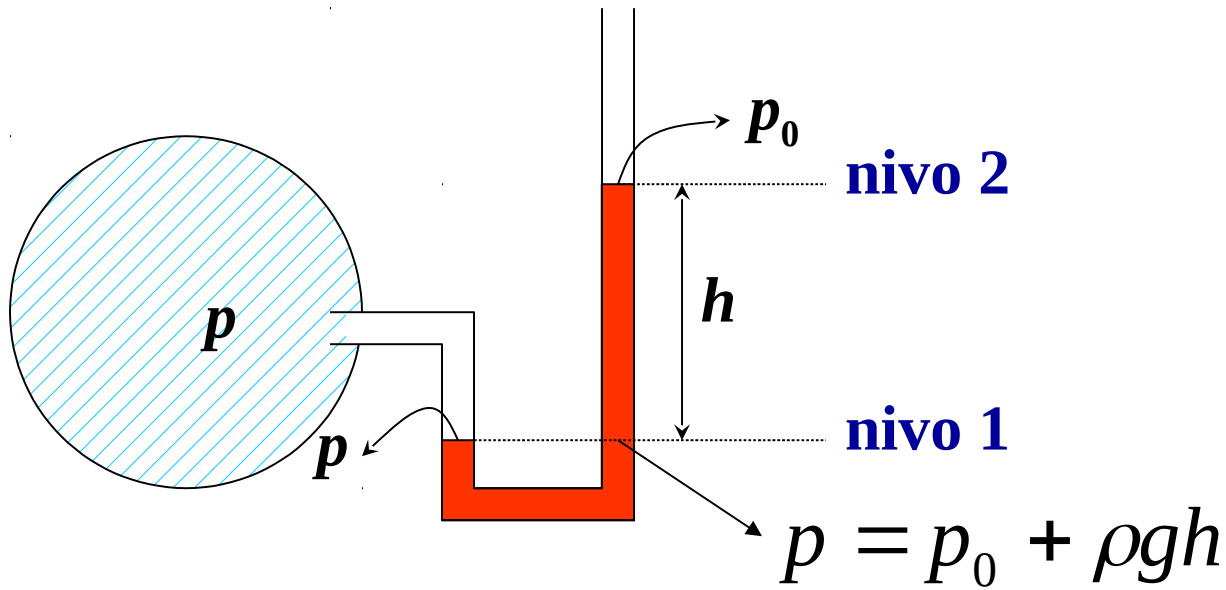


$$p_0 = \rho g h$$

merimo \rightarrow izračunamo
tlak



manometer

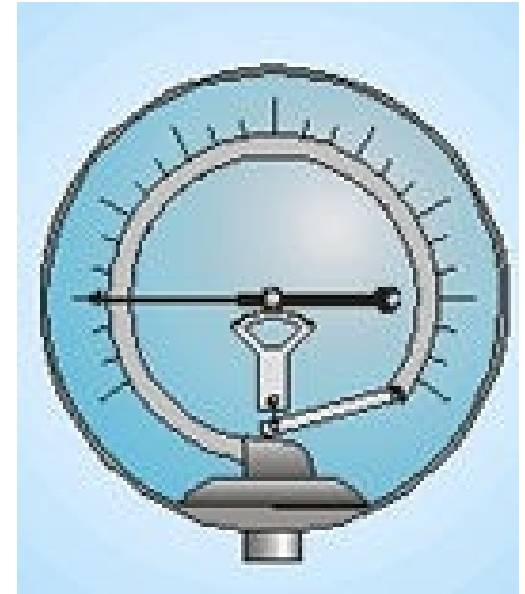


$$p - p_0 = \Delta p = \rho gh$$

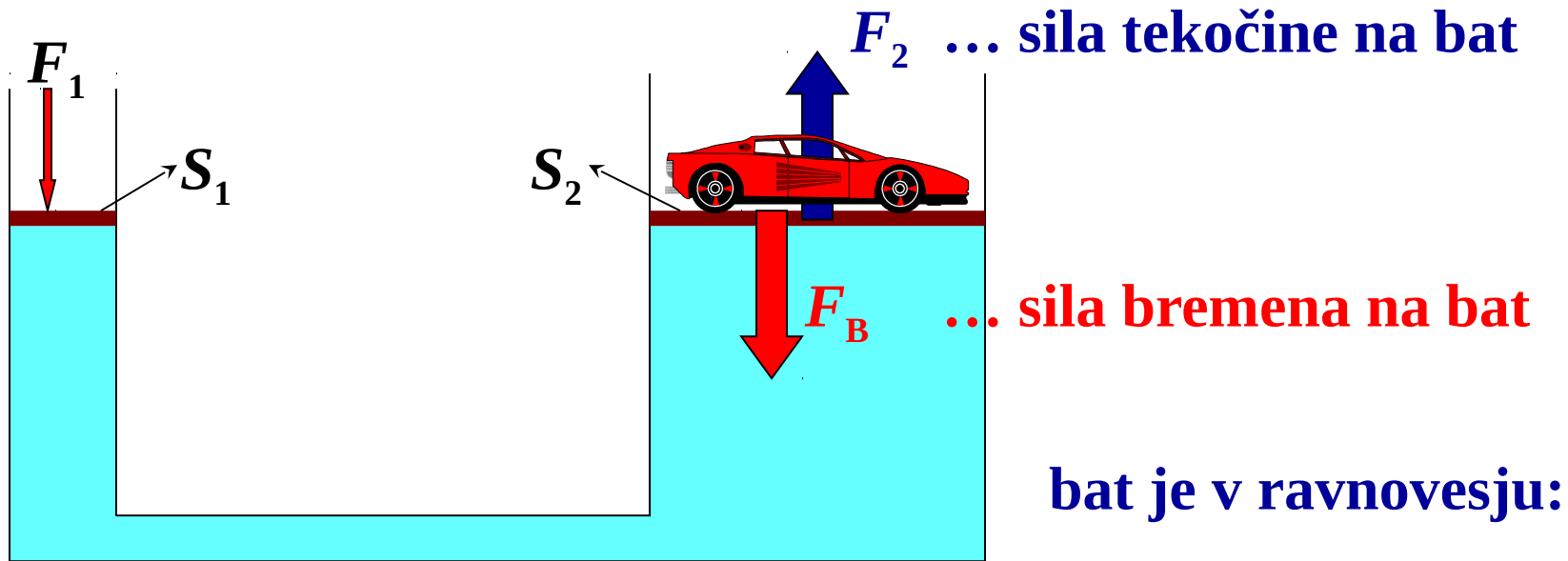
razlika tlakov

višinska razlika med gladinama

Bourdonova cevka



PASCALOVO NAČELO



$$F_2 = F_B$$

tlak pod levim batom se poveča:

$$\Delta p = \frac{F_1}{S_1}$$

Pascal

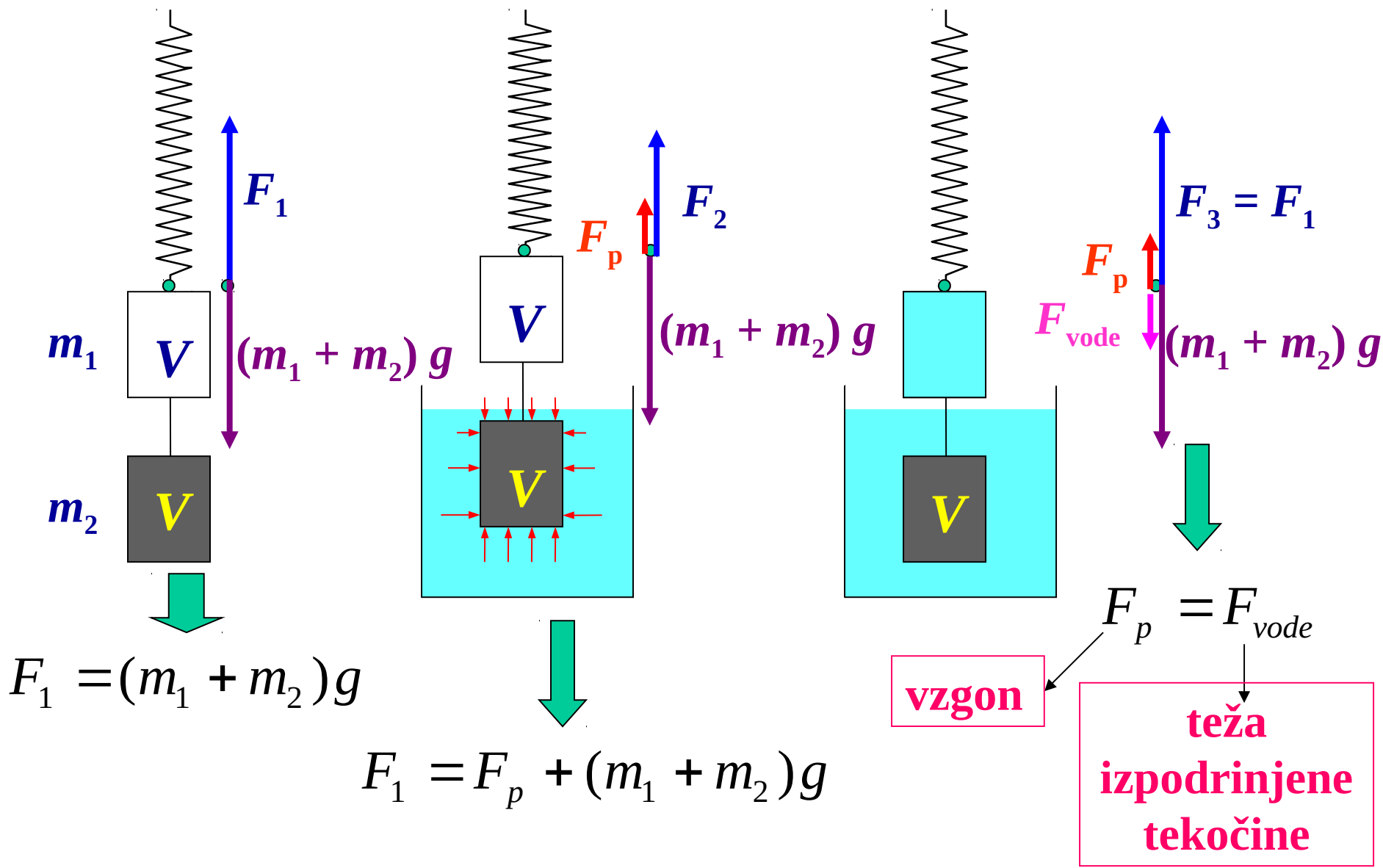


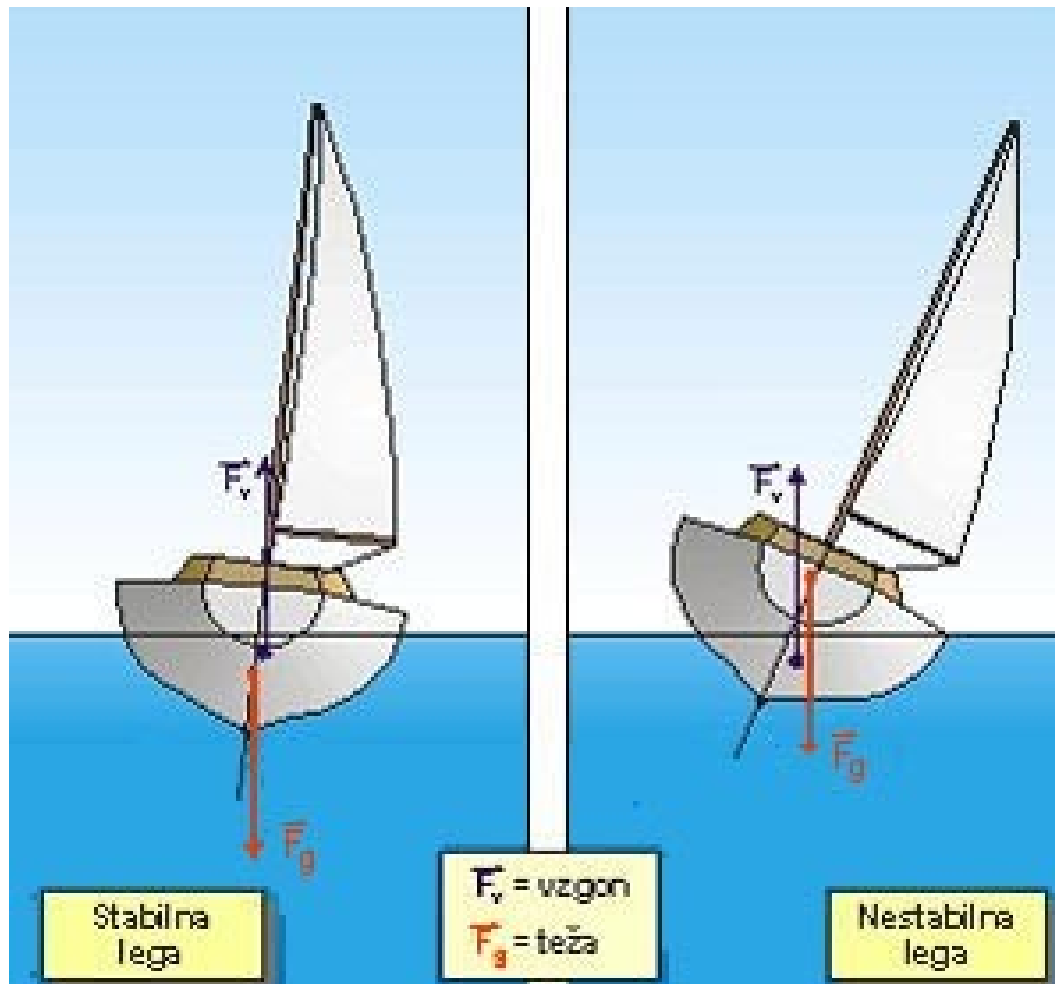
poveča se tlak pod drugim batom:

$$\Delta p = \frac{F_2}{S_2}$$

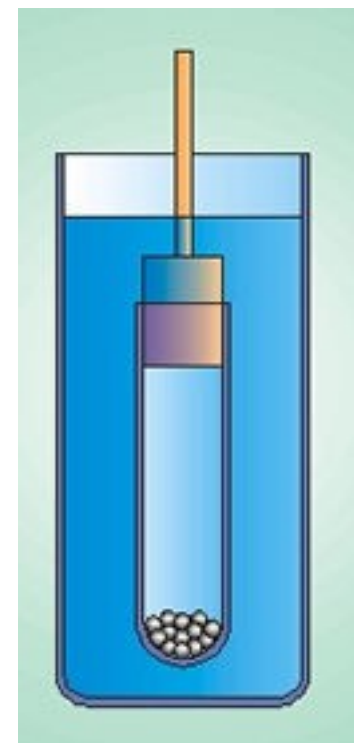
$$\frac{F_1}{S_1} = \frac{F_2}{S_2}$$

ARHIMEDOV ZAKON





merilnik za
gostoto kapljevine



areometer

GIBANJE IDEALNIH TEKOČIN

približki:

1. laminarni tok



2. nestisljiva tekočina: $\rho = \text{konst.}$

3. neviskozna tekočina: ni trenja med sosednjimi plastmi tekočine

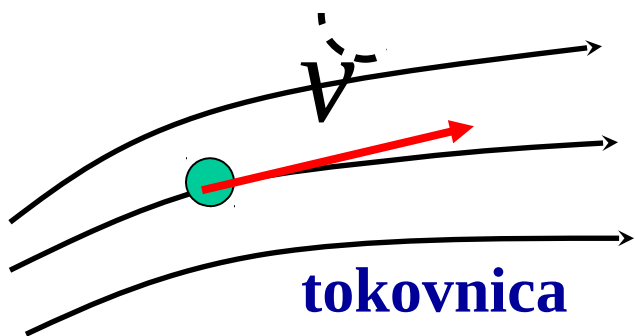
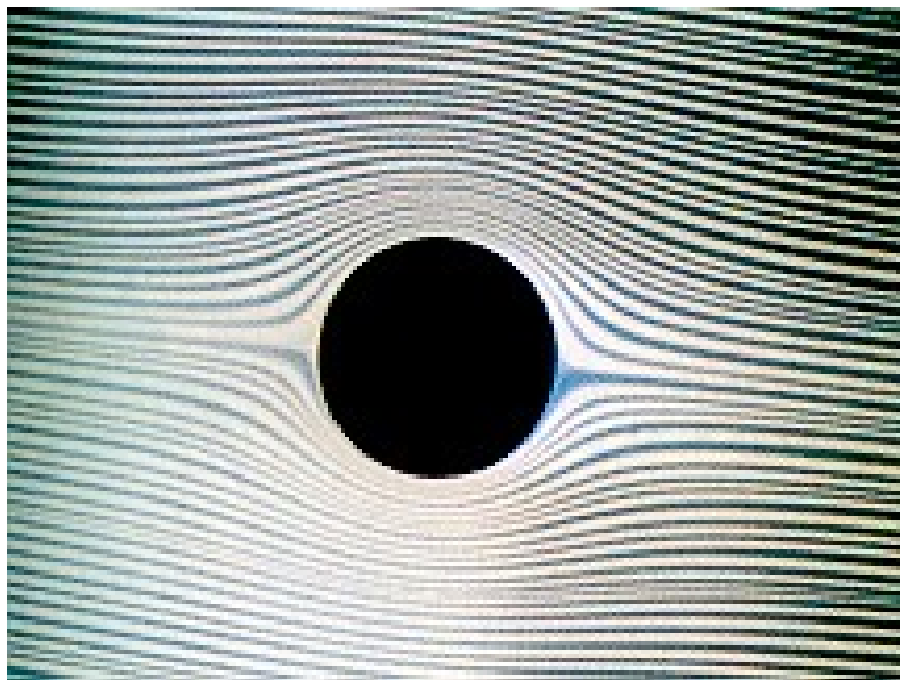
4. irotacionalno gibanje

KONTINUITETNA ENAČBA

tokovnica



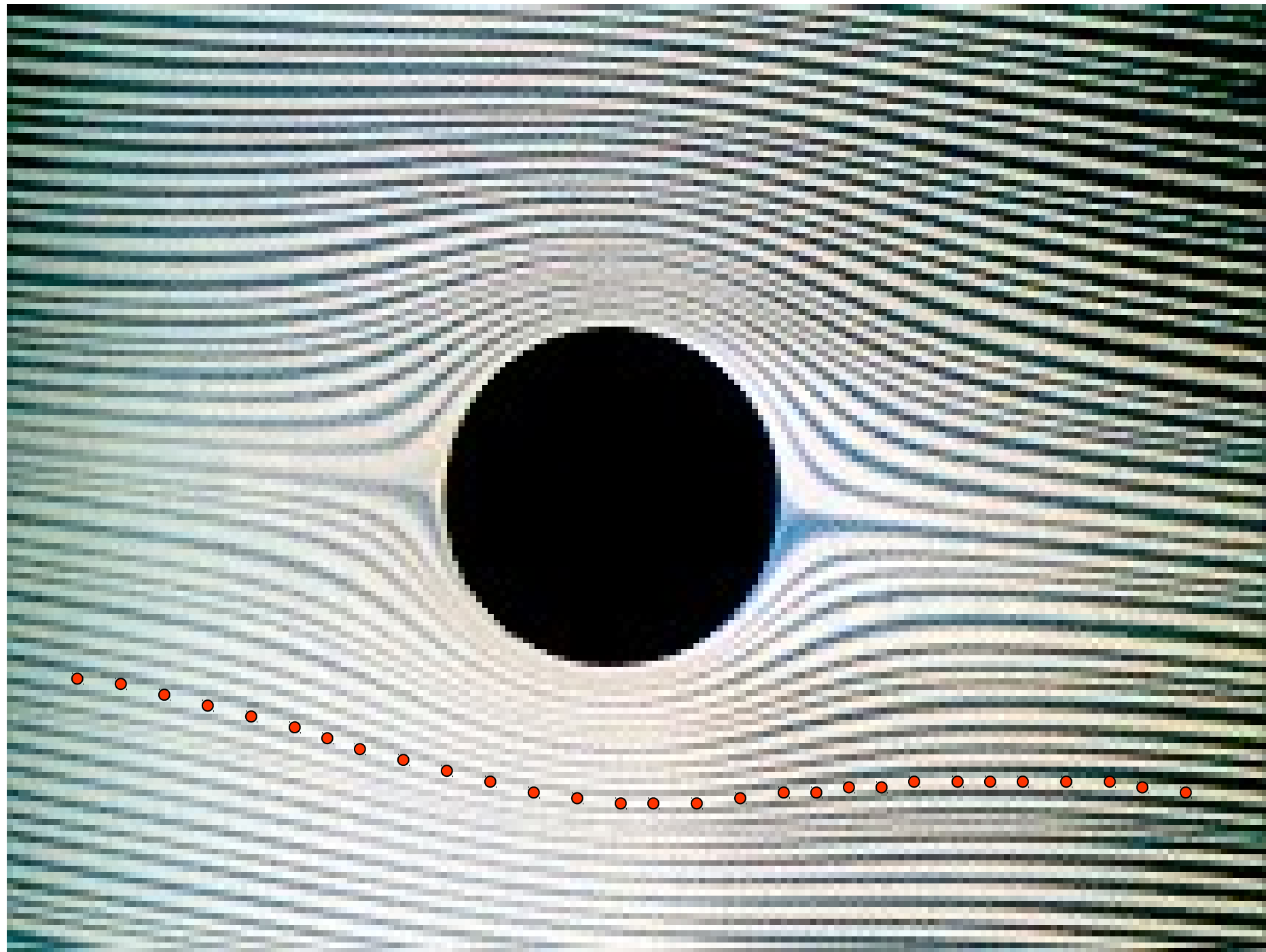
pot, ki ji sledi delček tekočine



tokovnica

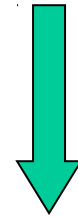
vektor hitrosti je vedno tangenten na tokovnico

tokovnice se nikoli ne sekajo

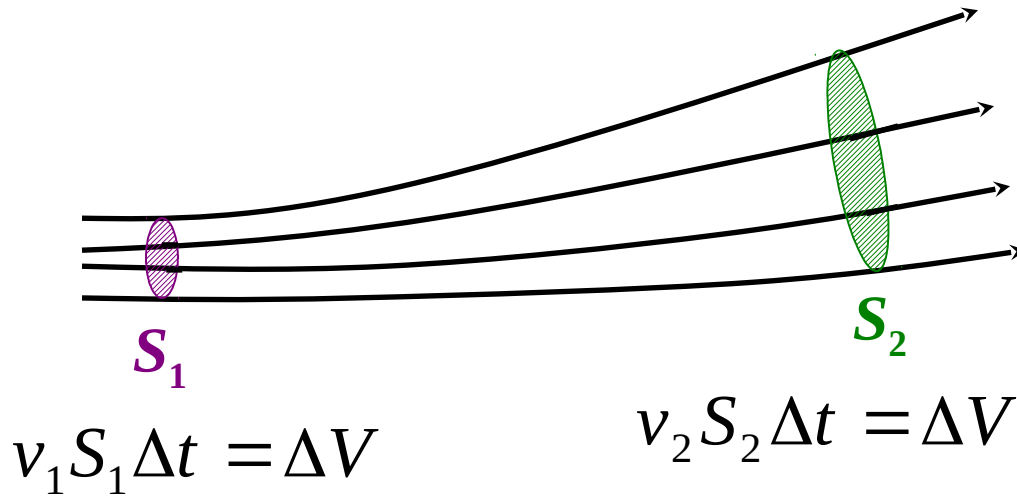


kontinuitetna enačba

$$v_1 S_1 = v_2 S_2$$



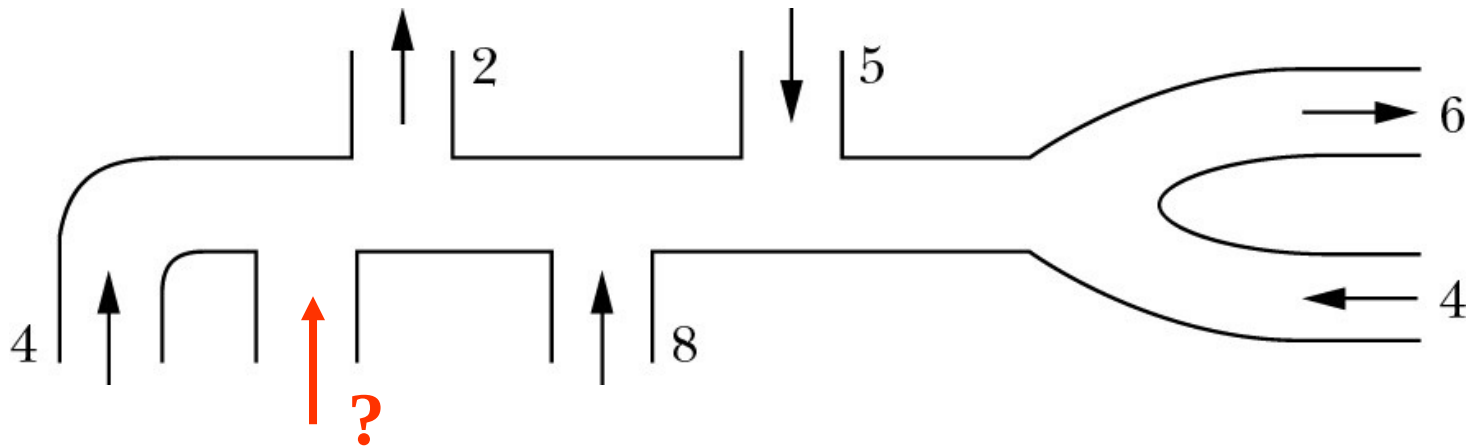
zakon o ohranitvi mase



$$\Phi_V = \frac{\Delta V}{\Delta t} = vS \quad \dots \text{volumski pretok}$$

$$\rho \Phi_V = \Phi_m \quad \dots \text{masni pretok}$$

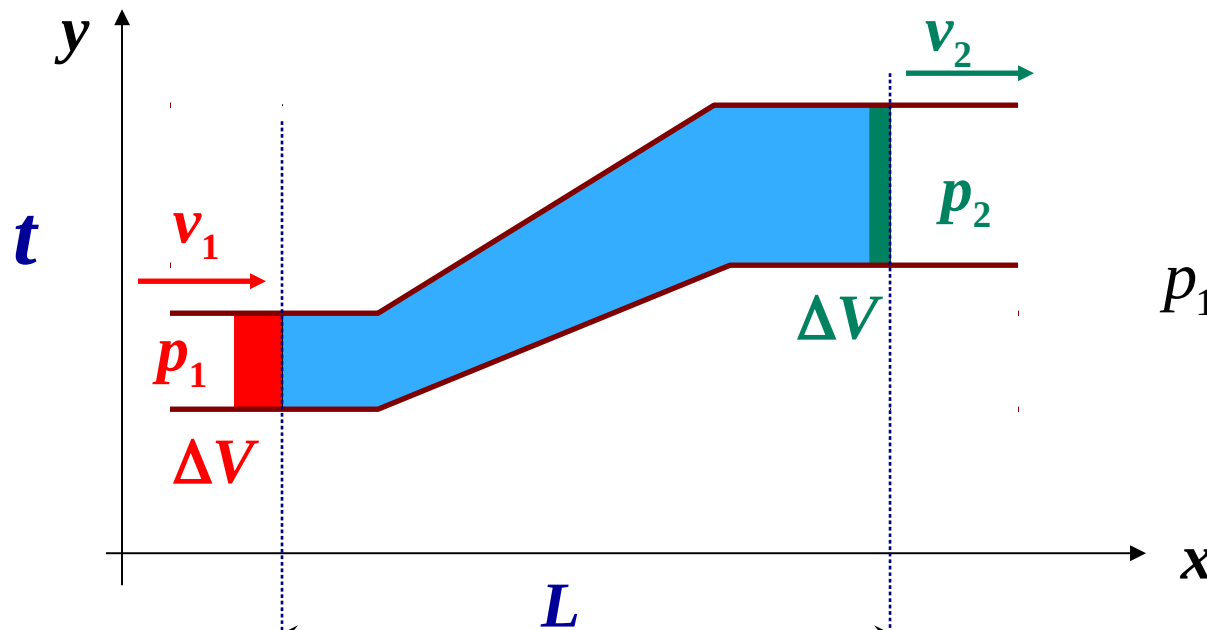
PRIMER:



PRIMER:

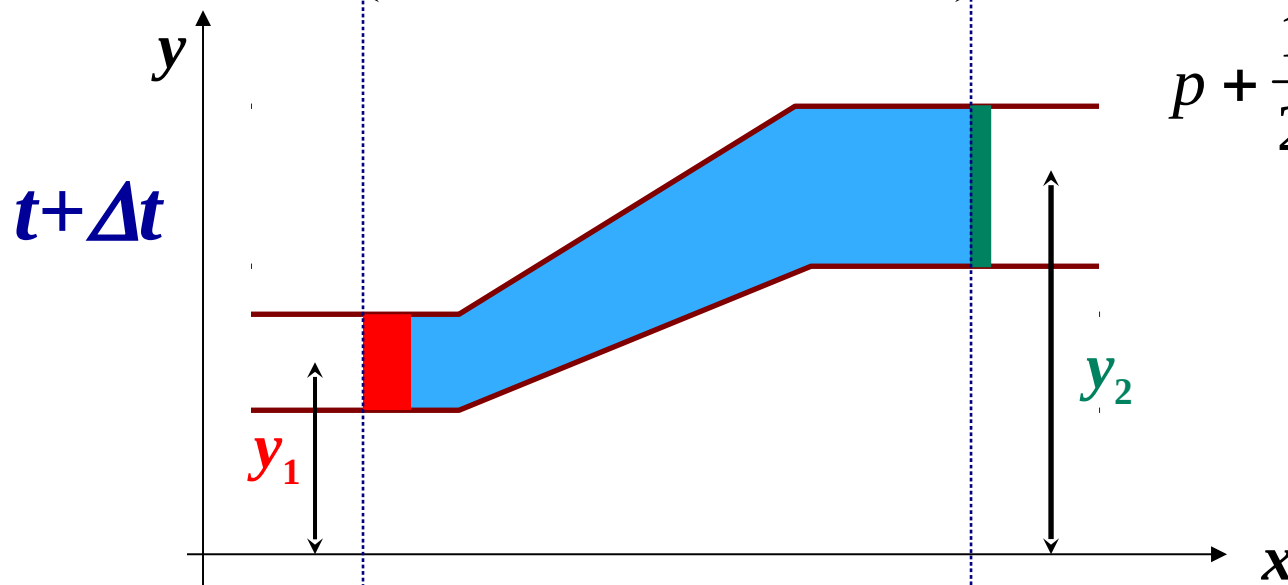
Presek aorte pri neki osebi je $3,0 \text{ cm}^2$, hitrost krvi po aorti je 30 cm/s . Presek kapilare je $3,0 \cdot 10^{-7} \text{ cm}^2$ in hitrost pretakanja krvi po kapilari $0,050 \text{ cm/s}$. Koliko kapilar ima ta oseba?

BERNOULLIJEVA ENAČBA



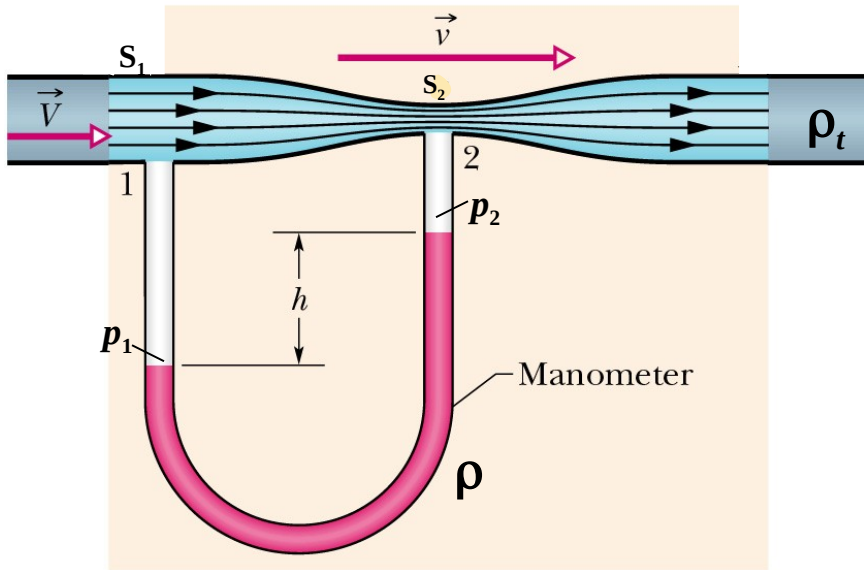
zakon o ohranitvi energije:

$$p_1 + \frac{1}{2} \rho v_1^2 + \rho g y_1 = p_2 + \frac{1}{2} \rho v_2^2 + \rho g y_2$$

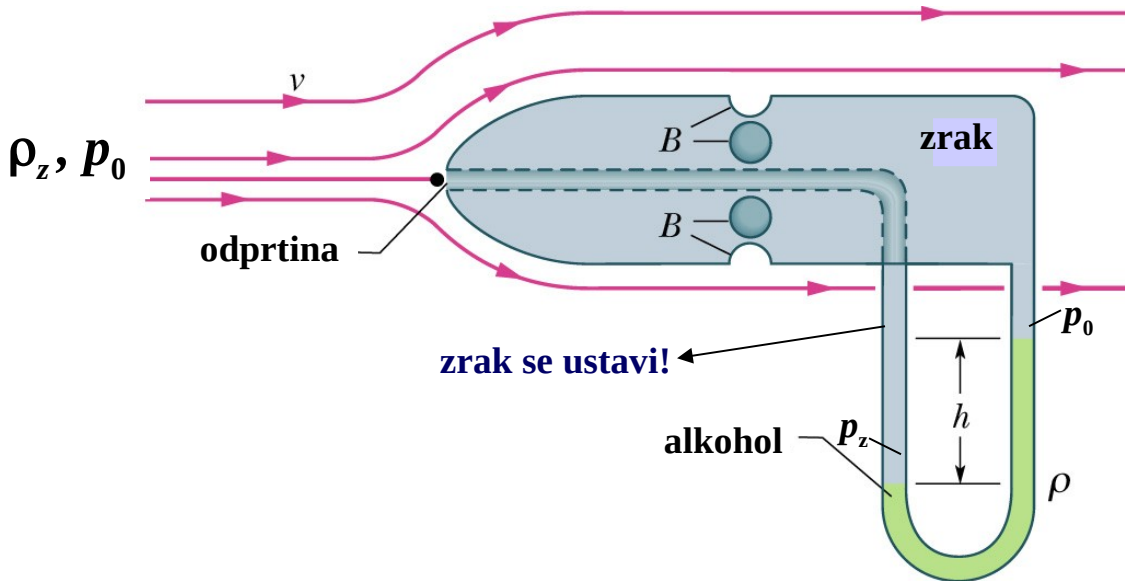


$$p + \frac{1}{2} \rho v^2 + \rho g y = \text{konst}$$

MERJENJE HITROSTI TEKOČINE



VENTURIJEVA CEV



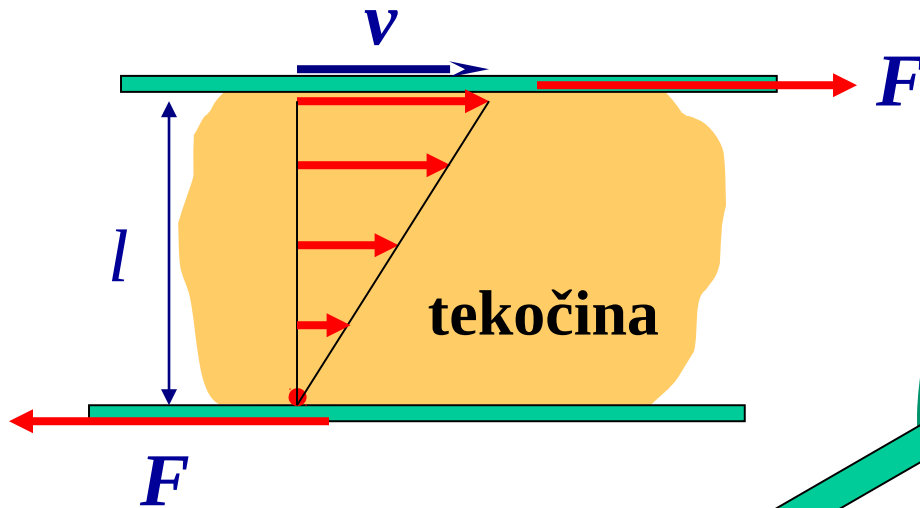
PITOTOVA CEV

$$p_z - p_0 \quad \text{zastojni tlak}$$

VISKOZNOST

kapljevina: **kohezivne sile** med molekulami

plin: **trki** med molekulami



tekočino strižno obremenimo

strižna napetost

$$\frac{F}{S} = \eta \frac{v}{l}$$

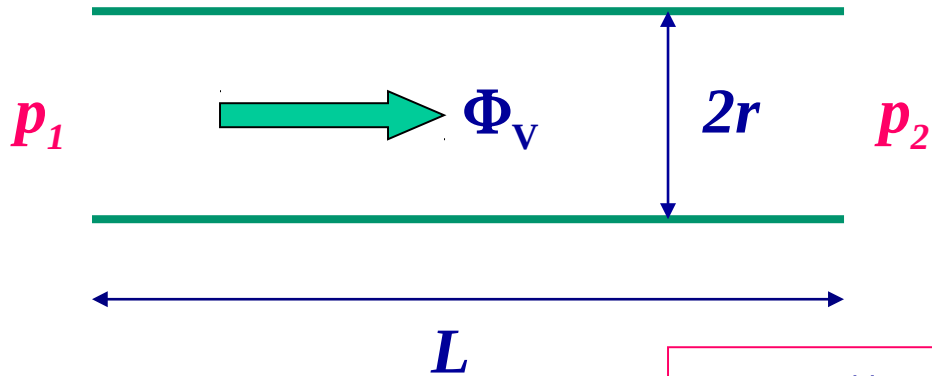
strižna hitrost

$$\left[\frac{\text{g}}{\text{cms}} \right] = 1 \text{ poise}$$

viskoznost

$$\left[\frac{\text{kg}}{\text{ms}} = \text{Pas} \right]$$

TOK TEKOČINE PO CEVI



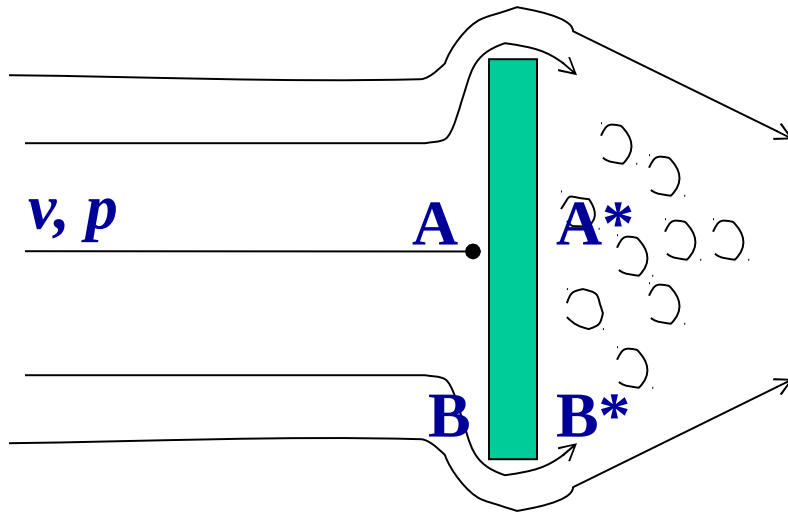
drastičen vpliv !

$$\Phi_v = \frac{\pi r^4 (p_2 - p_1)}{8 \eta L}$$

The equation is annotated with green circles and arrows. A green circle around r^4 has an arrow pointing up to the text "drastičen vpliv !". A green circle around the entire fraction $\frac{\pi r^4 (p_2 - p_1)}{8 \eta L}$ has an arrow pointing down to the text "gradient tlaka".

gradient tlaka

UPOR



$$\underbrace{p_A - p_{A^*}} > p_B - p_{B^*}$$

$\approx p_A - p$...zastojni tlak v točki A

$$p + \frac{1}{2} \rho v^2 = p_A$$

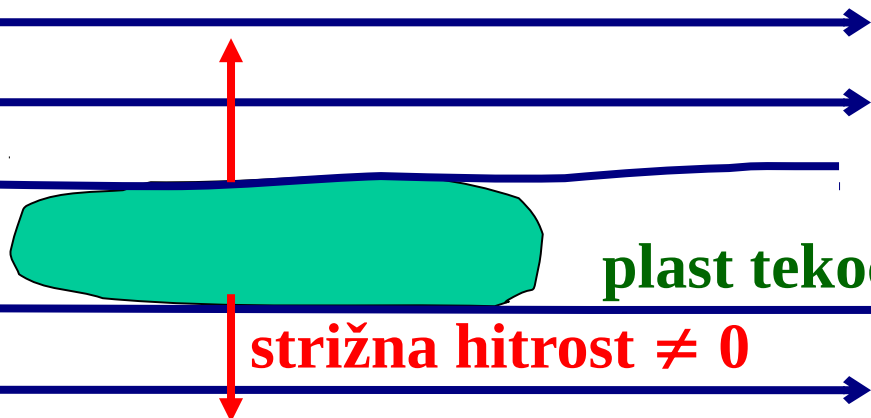
sila na ploščo:

$$F \approx (p_A - p_{A^*}) S$$

$$F \propto \rho v^2 S$$

$$F = \frac{1}{2} c_u \rho v^2 S$$

SILA NA TELO ZARADI VISKOZNOSTI OKOLNE TEKOČINE



plast tekočine ob telesu miruje

strižna hitrost $\neq 0$

$$\frac{F}{S} = \eta \frac{v}{l} \quad \text{ali} \quad \frac{F}{S} = \eta \frac{dv}{dl}$$

krogla:

$$S \approx 4\pi R^2$$

$$\frac{dv}{dl} \approx \frac{v}{R}$$

$$F \approx 4\pi\eta Rv$$

... ocena

natančen izračun:

$$F = 6\pi\eta Rv$$

Stokes

upor drugih teles:

značilna razsežnost v čelnem preseku

linearni zakon upora

$$F = \text{koeficient} \cdot \eta \cdot l \cdot v$$

velja za laminarni tok

odvisen od telesa

rel. hitrost telesa
glede na tekočino

Kdaj velja linearni in kdaj kvadratni zakon upora?

majhne v

velike v

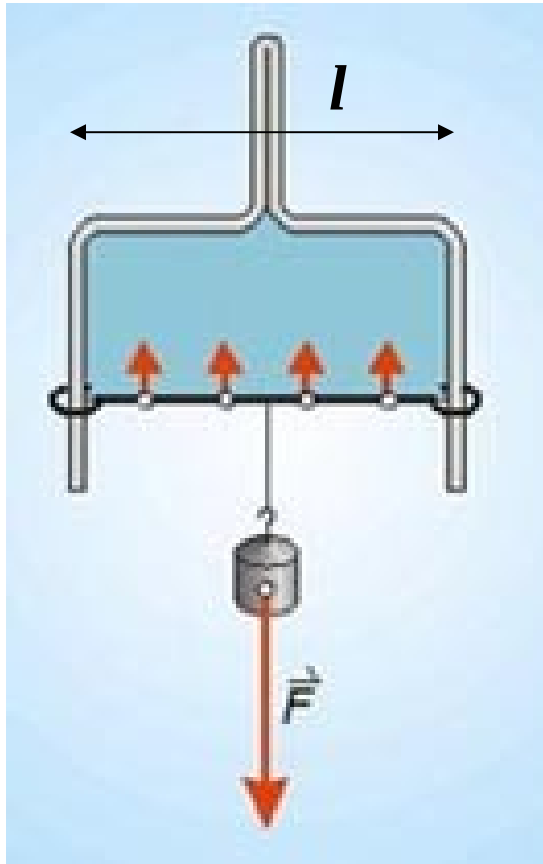
$$\frac{F_u^{\text{kvadratni}}}{F_u^{\text{linearni}}} \approx \frac{v^2 R^2 \rho}{\eta v R} \quad \text{DEF:} \quad \text{Re} = \frac{v \rho l}{\eta} \quad \text{Reynoldsovo število}$$

Re < 0,5 ... linearni zakon upora

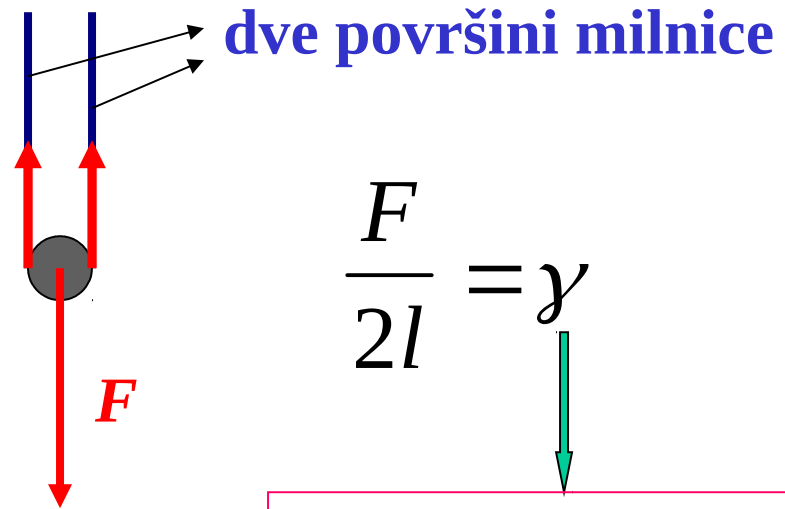
Re > 1000 ... kvadratni zakon upora

vmes ... uporaba tabel

POVRŠINSKA NAPETOST



pogled od strani:



$$\frac{F}{2l} = \gamma$$

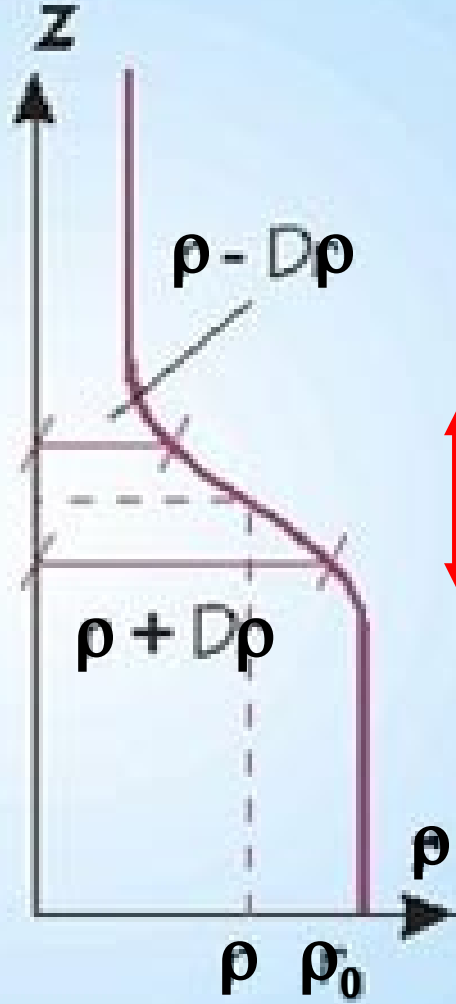
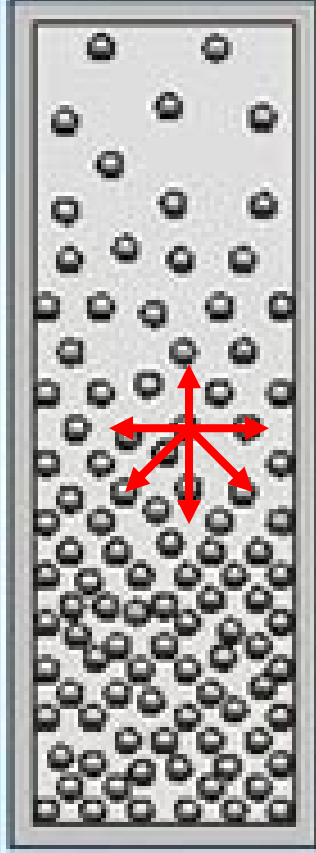
površinska napetost

sila na dolžinsko enoto, ki poskuša prečko potegniti gor, t.j. zapreti površino

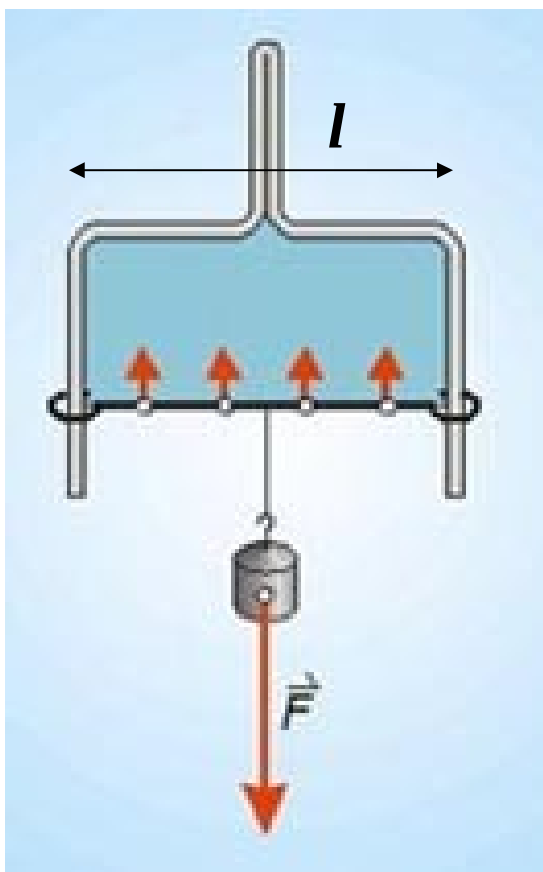
H₂O pri 20°C: $\gamma = 0,072$ N/m

milnica pri 20°C: $\gamma = 0,025$ N/m

**kapljevina postopoma
prehaja v paro**



**nekaj nm debela,
neenakomerno gosta plast**



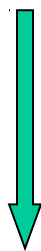
površino želimo povečati:

opraviti moramo delo:

$$A = F \Delta x$$

$$A = \gamma L \Delta x \quad L = 2l$$

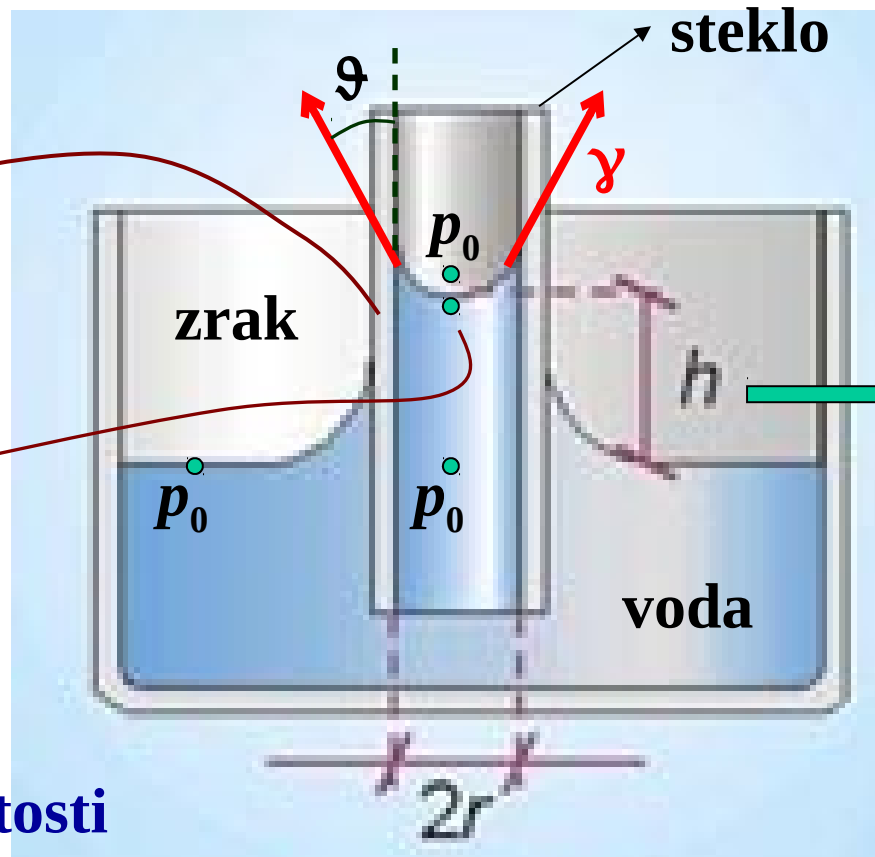
$$A = \gamma \Delta S = \gamma S_2 - \gamma S_1$$



površinska energija

poveča potencialno energijo molekul

KAPILARNI DVIG



tri površine
⇒ tri γ

$$p_0 - \rho gh$$



razliko nadomesti tlak
zaradi površinske napetosti

$$F_y \cos \vartheta = S \Delta p$$

$$\gamma 2\pi r \cos \vartheta = \pi r^2 \rho gh$$

$$h = \frac{2\gamma \cos \vartheta}{rg\rho}$$

voda omoči steklo



adhezivne sile večje od kohezivnih

živo srebro ne omoči stekla



kohezivne sile večje
od adhezivnih

