

Potence, korenji

$$\begin{aligned}\int x^n dx &= \frac{x^{n+1}}{n+1} + C \quad \text{pri } n \neq -1 \\ \int x^{-1} dx &= \int \frac{dx}{x} = \ln|x| + C \\ \int \sqrt{x} dx &= \frac{2}{3}x\sqrt{x} + C \\ \int \frac{1}{\sqrt{x}} dx &= 2\sqrt{x} + C \\ \int \frac{1}{\sqrt{1-x^2}} dx &= \arcsin x + C \\ \int \frac{x}{\sqrt{x^2-1}} dx &= \operatorname{arcsec} x + C\end{aligned}$$

Polinomi, racionalne funkcije

$$\begin{aligned}\int (ax+b) dx &= \frac{ax^2}{2} + bx + C \\ \int (ax^2+bx+c) dx &= \frac{a}{2}x^3 + \frac{b}{2}x^2 + cx + C \\ \int (ax+b)^n dx &= \frac{(ax+b)^{n+1}}{a(n+1)} + C \\ \int \frac{dx}{ax+b} &= \frac{1}{a} \ln|ax+b| + C \\ \int \frac{1}{x^2+1} dx &= \arctan x + C \\ \int \frac{dx}{x^2+a^2} &= \frac{1}{a} \arctan \frac{x}{a} + C \\ \int \frac{f'(x)}{f(x)} dx &= \ln|f(x)| + C\end{aligned}$$

Eksponentne, logaritemske funkcije

$$\begin{aligned}\int e^x dx &= e^x + C \\ \int a^x dx &= \frac{a^x}{\ln a} + C \\ \int xe^x dx &= e^x(x-1) + C \\ \int \frac{dx}{e^x} &= -\frac{1}{e^x} + C \\ \int \frac{x}{e^x} dx &= -\frac{x+1}{e^x} + C \\ \int \frac{e^x}{x} dx &= -Ei(-x) + C \quad \text{Opomba: Ei = eksponentni integral} \\ \int \ln x dx &= x \ln x - x + C \\ \int \log_a x dx &= x \log_a x - \frac{x}{\ln a} + C\end{aligned}$$

Trigonometrične funkcije

$$\begin{aligned}\int \cos x dx &= \sin x + C \\ \int \cos(nx) dx &= \frac{\sin(nx)}{n} + C \\ \int \sin x dx &= -\cos x + C \\ \int \sin(nx) dx &= -\frac{\cos(nx)}{n} + C \\ \int \tan x dx &= -\ln|\cos x| + C \\ \int \csc x dx &= -\ln|\csc x + \cot x| + C \\ \int \sec x dx &= \ln|\sec x + \tan x| + C \\ \int \cot x dx &= \ln|\sin x| + C \\ \int \frac{dx}{\cos^2 x} &= \int \sec^2 x dx = \tan x + C \\ \int \frac{dx}{\sin^2 x} &= \int \csc^2 x dx = -\cot x + C \\ \int \sin^2 x dx &= \frac{2x - \sin 2x}{2} + C = \frac{x}{2} - \frac{\sin 2x}{2} + C \\ \int \cos^2 x dx &= \frac{2x + \sin 2x}{2} + C = \frac{x}{2} + \frac{\sin 2x}{4} + C\end{aligned}$$

$$\begin{aligned}\int_0^\infty \frac{1}{x^2+a^2} dx &= \frac{\pi}{2a} \\ \int_0^\infty \frac{1}{(1+x)a^2} dx &= \frac{\pi}{\sin(a\pi)}, \quad (a < 1) \\ \int_0^\infty \frac{1}{x^{a-1}} dx &= \frac{\pi}{\sin(a\pi)}, \quad (0 < a < 1) \\ \int_0^\infty \frac{1}{(1-x)a^a} dx &= -\pi \operatorname{ctg}, \quad (a < 1) \\ \int_{-\infty}^\infty \frac{1}{(1+x^2/a)^{(a+1)/2}} dx &= \frac{\sqrt{a\pi} \Gamma(a/2)}{\Gamma((a+1)/2)}, \quad (a > 0) \quad (\text{povezava z gostoto verjetnosti Studentove t-pore}) \\ \int_0^\infty \frac{x^{a-1}}{1+b^2x^2} dx &= \frac{\pi}{b \sin(a\pi/b)}, \quad (0 < a < b) \\ \int_0^\infty \frac{x^a}{x^b+c^b} dx &= \frac{\pi c^{a+1-b}}{b \sin[(a+1)\pi/b]}, \quad (0 < a+1 < b) \\ \int_0^\infty \frac{x^a}{(x^b+c^b)^d} dx &= \frac{(-1)^{d-1} \pi c^{a+1-bd}}{b \sin[(a+1)\pi/b] (d-1)! \Gamma[(a+1)/(b-d+1)]}, \quad (0 < a+1 < bd) \\ \int_0^\infty \frac{1}{1+2x \cos(a)+x^2} dx &= \frac{a}{\sin a} \\ \int_0^\infty \frac{x^b}{1+2x \cos(a)+x^2} dx &= \frac{\pi}{\sin(b\pi)} \frac{\sin(ab)}{\sin a}, \quad \left(0 < a < \frac{\pi}{2}\right)\end{aligned}$$

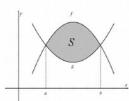
If $u = f(x)$, $v = g(x)$, and the differentials $du = f'(x) dx$ and $dv = g'(x) dx$, then the product rule in its simplest form is:

$$\int u \frac{dv}{dx} dx = uv - \int v \frac{du}{dx} dx$$

Prostornina:

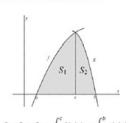
$$V = \pi \int_a^b f^2(x) dx$$

Pločina lika med dvema krivuljama



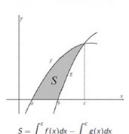
$$S = \int_a^b (f(x) - g(x)) dx$$

Pločina lika kot vsota dveh pločin likov



$$S = S_1 + S_2 = \int_a^c f(x) dx + \int_c^b g(x) dx$$

Rčina lika med dvema krivuljama in x osjo



$$S = \int_a^b f(x) dx - \int_a^b g(x) dx$$